

A Mixed-Integer Linear Optimization Approach for Power-to-X-Technologies in a District Heating System

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Overview



- **Introduction**
- **Energy Hub**
- **Optimization Model**
- **Results**
- **Conclusions**



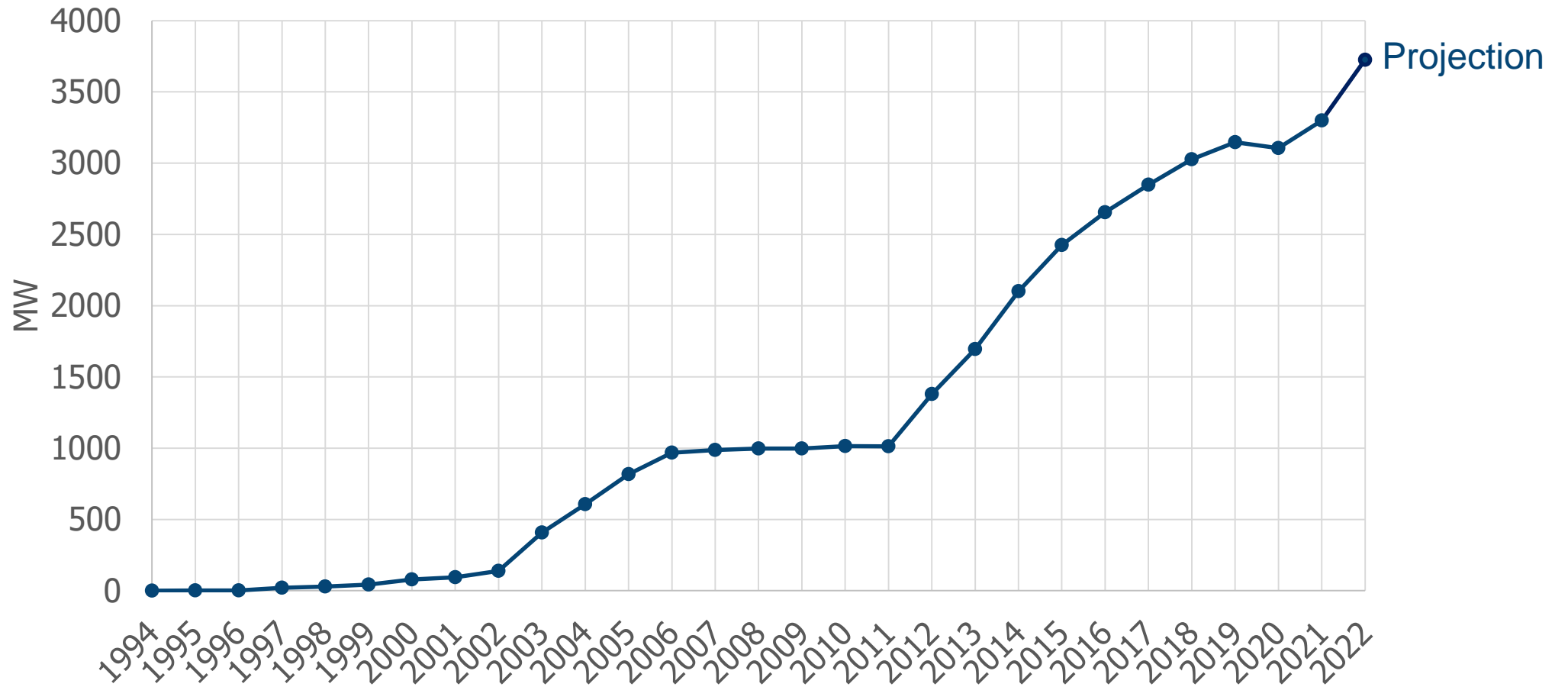
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Wind Power in Austria

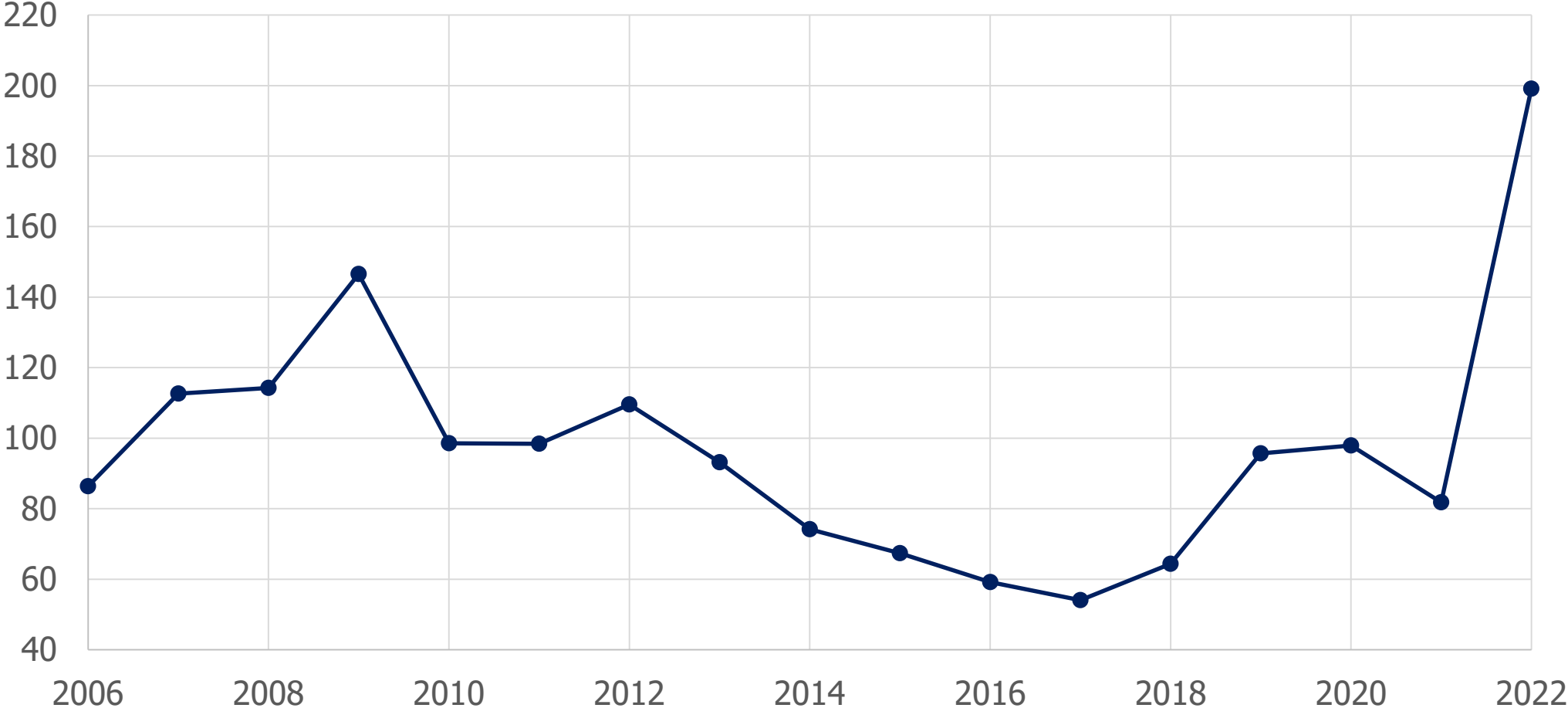


Source: IG Windkraft, January 2022.

Electricity Price



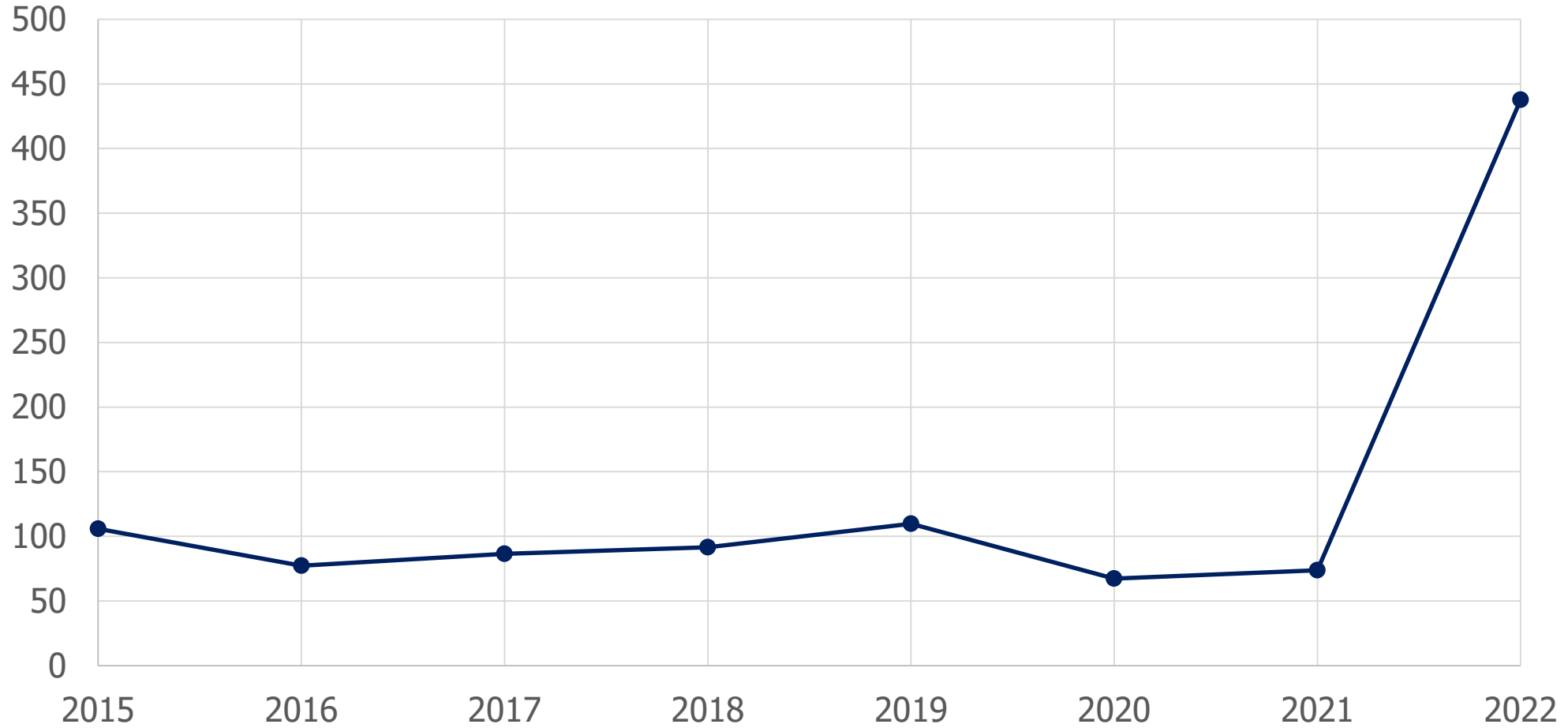
ÖSPI



Gas Price



ÖGPI



Introduction



■ Motivation

- Subsidized feed-in tariffs are limited in time
- Transition of energy systems only possible with sector coupling
 - Coupling of electricity with heat sector in district heating networks (power-to-heat)
 - Coupling with gas sector still challenging (power-to-gas)
 - Integration of electrolyzers yields potential to produce green hydrogen

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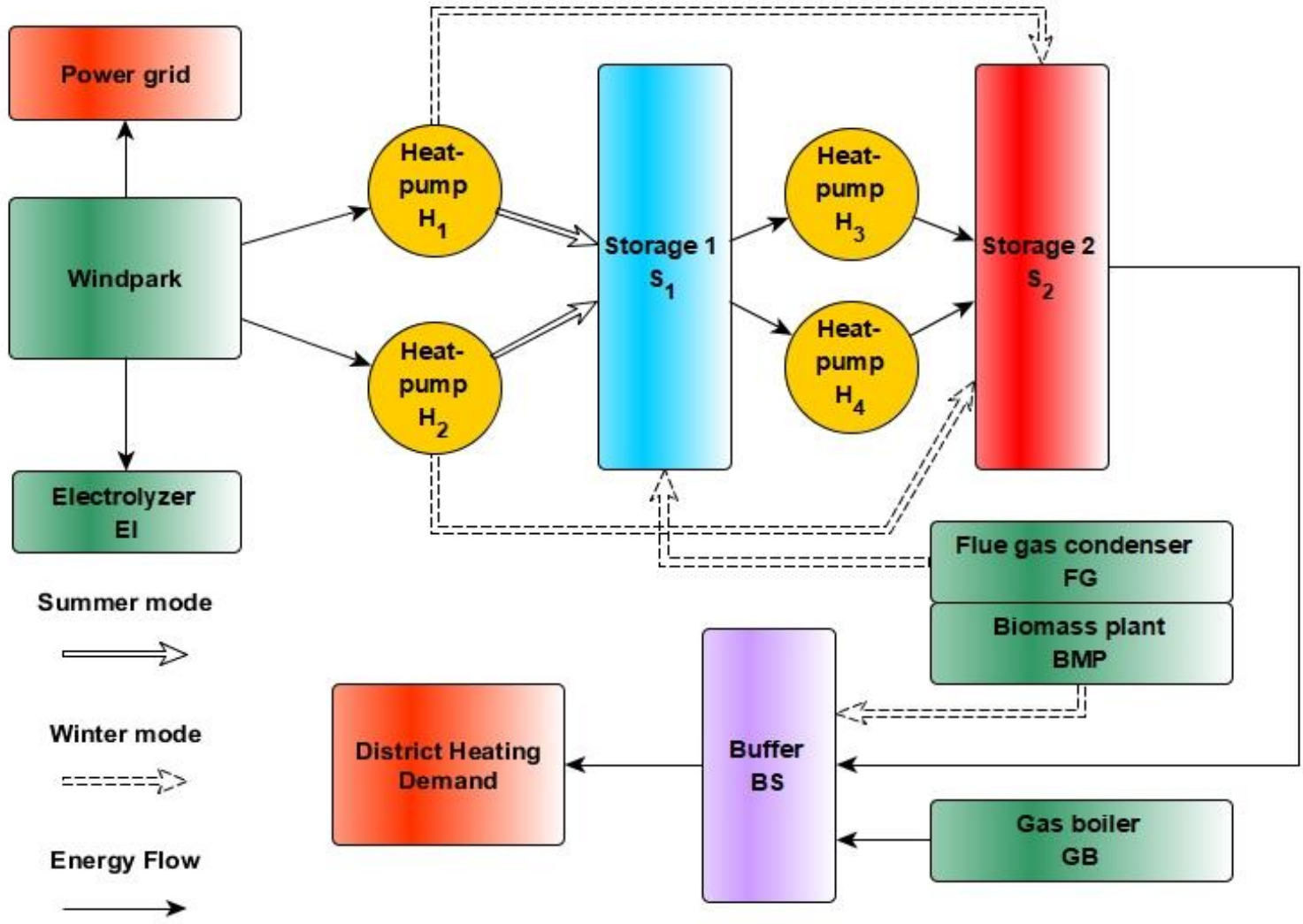
Energy Hub



■ Components

- Wind park
- Heat pumps
- Thermal storages
- Electrolyzer
- Biomass plant with flue gas condenser
- Gas boiler

Energy Hub



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Optimization Model



■ Overview

- System modeled using mixed-integer linear optimization approach
- Linearization and approximations necessary
- Components modelled in python utilizing pyomo¹
- Objective function minimizes yearls costs of energy hub

¹Bynum et al. *Pyomo – Optimization Modeling in Python*. 2nd edition. Vol 67. Springer, 2021.

■ Components I

- Heat pump model based on COP value $\dot{Q}_{th,HP}(t) = P_{el,HP}(t) \cdot COP_{HP}(t)$
- Biomass plant assumed to yield specific power at timestep t

- Utilized only in cold months

- Cost function $\min(\sum_t P_{th,BMP}(t) \cdot p_{BMP} \cdot \eta_{BMP}^{-1} \cdot T)$

- Flue gas condenser delivers share of biomass plant power

$$P_{th,FG}(t) = P_{th,BMP}(t) \cdot \eta_{FG}$$

■ Components II

- Gas boiler based on simple linear model with $P_{th,GB}$ and η_{GB}
 - Costs implemented directly in objective function $\min(P_{th,GK}(t) \cdot p_{GK} \cdot \eta_{GK}^{-1} \cdot T)$

- Grid connection allows for marketing wind energy

- Thermal storages modeled with simple linear approach

$$SOC_{st}(t) = SOC_{st}(t - 1) + T \cdot (SOC_{charge}(t) - SOC_{discharge}(t))$$

Overview



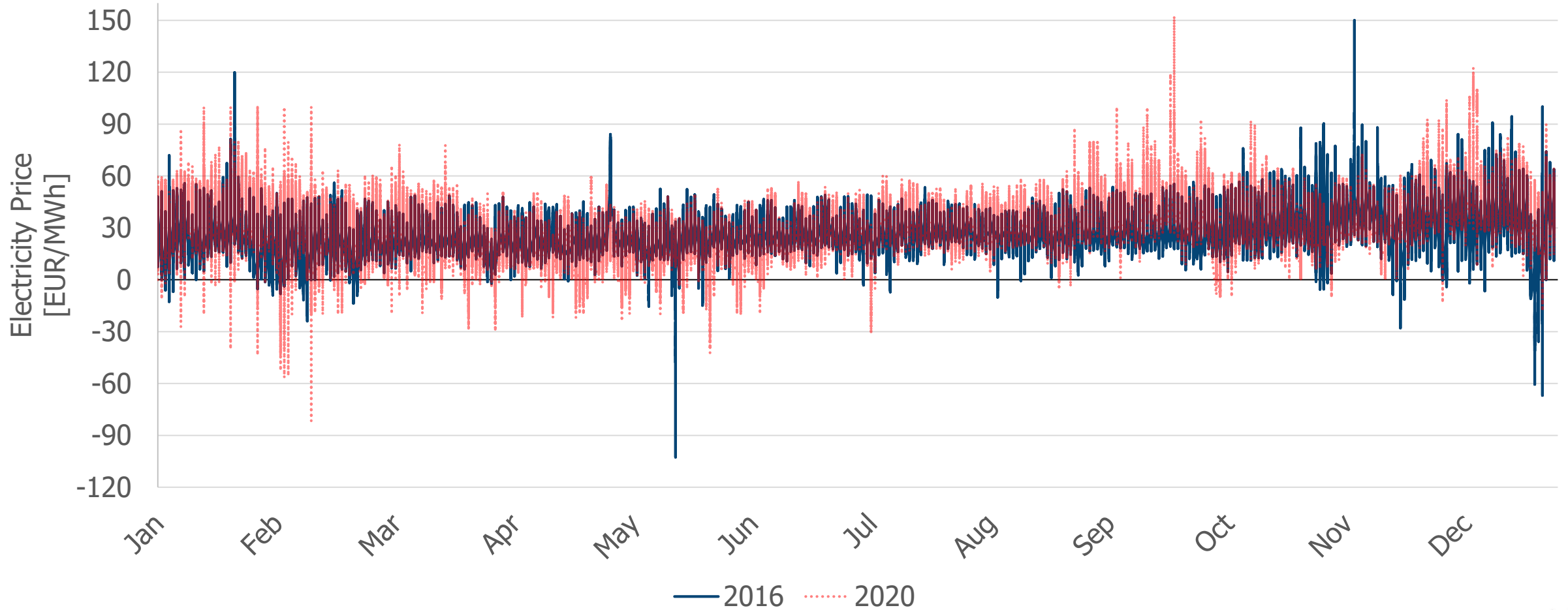
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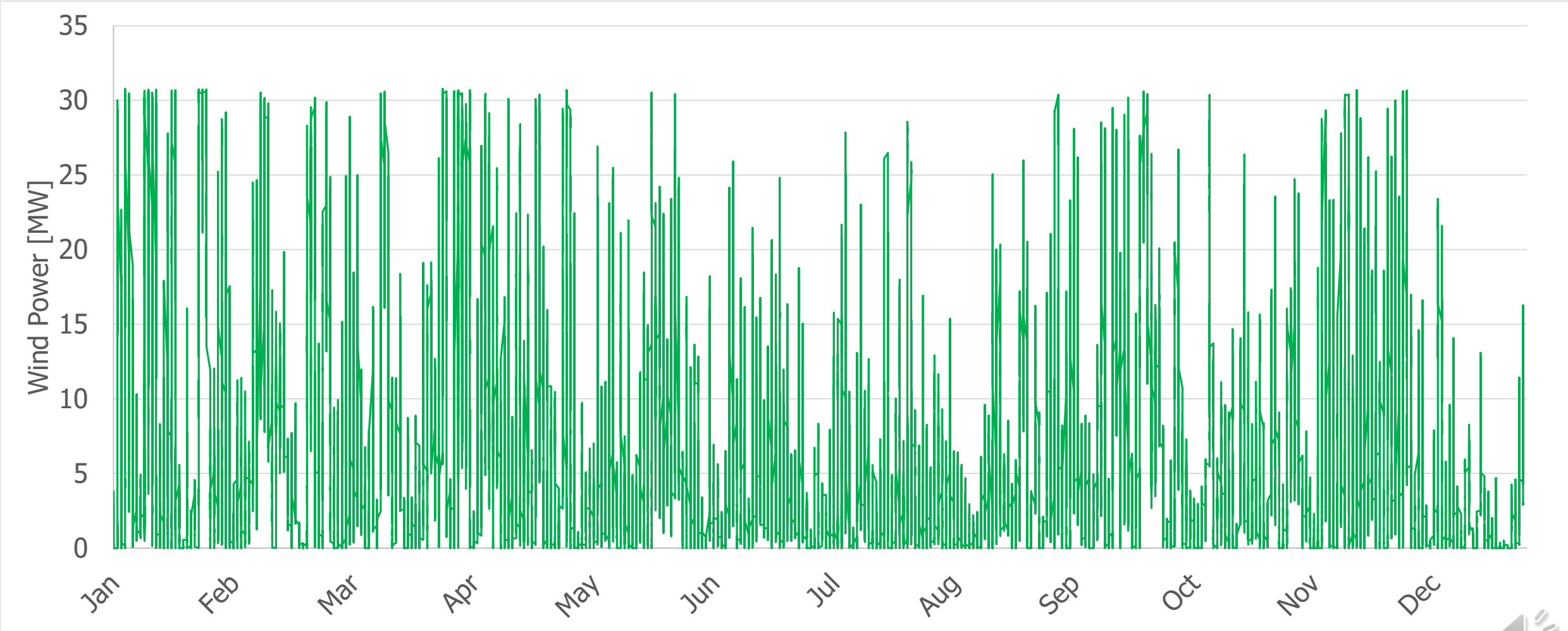
■ Model assumptions

- Aggregated heat pump power around 750 – 800 kW_{el}
- BMP power between 520 – 2,600 kW and a 15-min gradient of 780 kW
- Flue gas condenser with efficiency of 27 %
- GB maximum power at 3,900 kW
- Storage units with 13,300 l for S_1 and 18,200 l for S_2
- Buffer storage with 300,000 l
- Electrolyzer with 5,000 kW
- Hydrogen price assumed with 6 €/kg

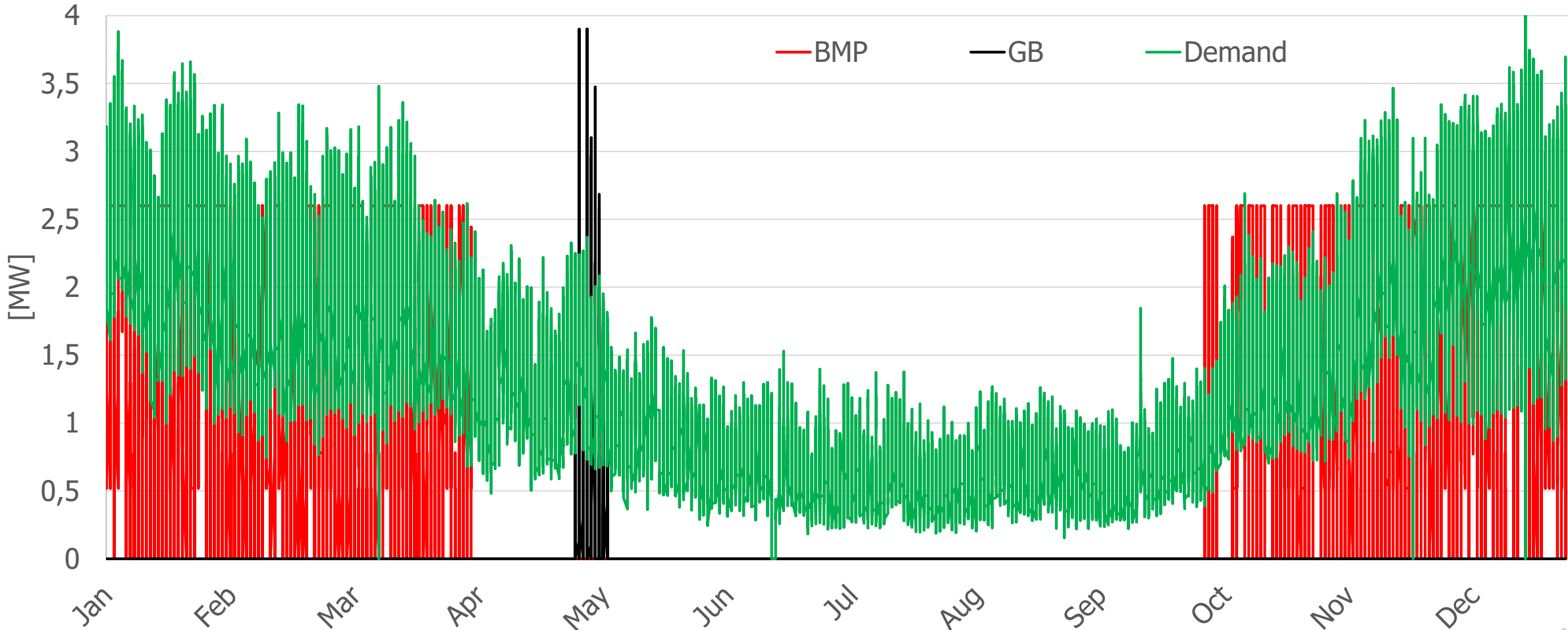
Results



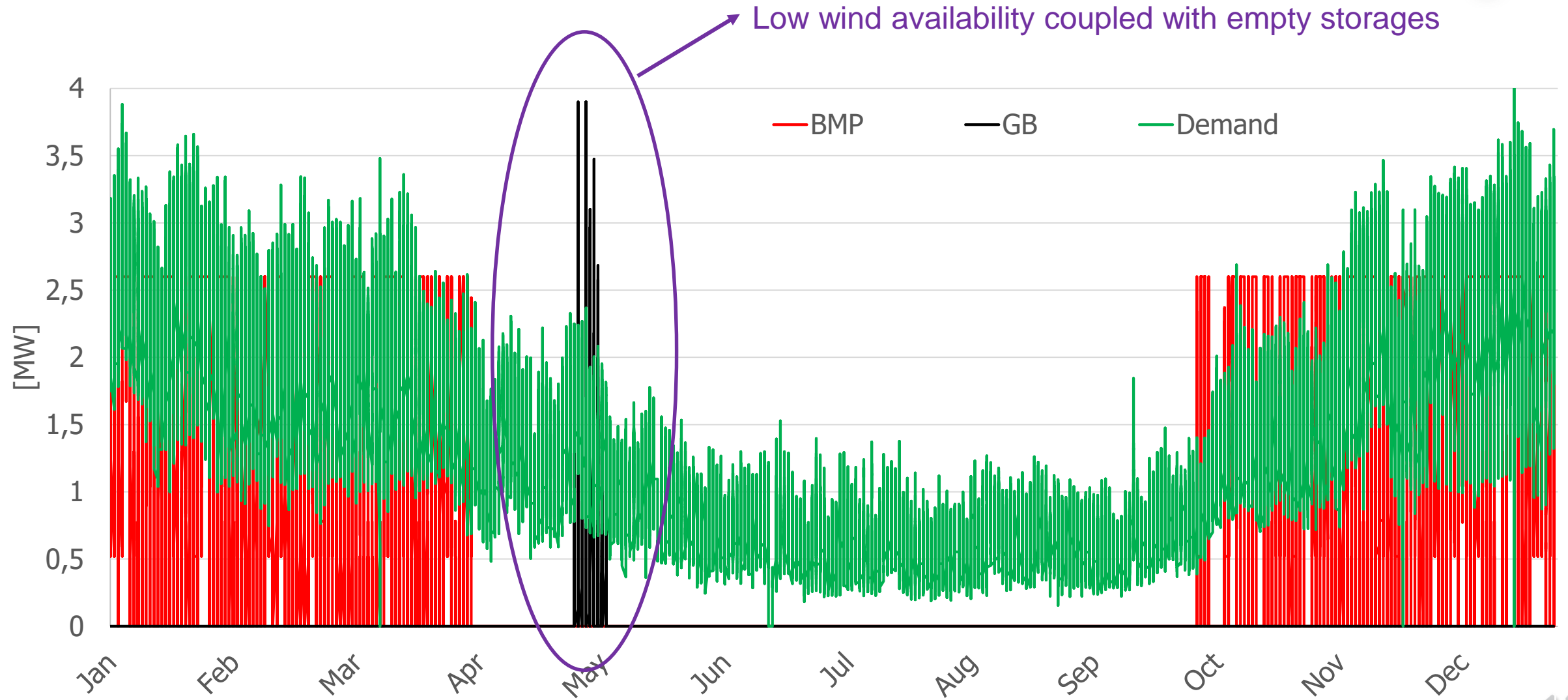
Results



Results



Results



▪ Electrolyzer

- Produces almost constantly hydrogen
- With the specified electrolyzer parameters around 18 t of hydrogen
- However, degradation and other technical effects not yet implemented in the optimization model

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Conclusions



- RESs can provide the lion's share of energy for an energy hub
- Backup solutions, e.g., gas, necessary
- Feasibility of electrolyzers depending on specific requirements
 - Hydrogen consumers
 - Storage and transportation options
 - Price of green, grey and black hydrogen
 - Technical details of electrolyzer technology